Fibonacci pinecone

Fibonacci packing Colouring schemes Pinecone shape

Second Life

What is it? Mathematical Art Math Education?

The Mathfest 2009 Poster Image, Mathematical Art, Design and Education in Second Life

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What is it? Mathematical Art Math Education? The basic pattern is this spiral of points, where the *n*th point is put down at radius \sqrt{n} and angle $2\pi\phi n$, where $\phi = \frac{\sqrt{5}-1}{2}$ is the golden ratio.

127 148 93 ¹¹⁴ ¹³⁵ 119 106 80 101 122 143 77 64 51 67 ⁸⁸ 56 43 137 103 54 75 48 35 22 $150 \ ^{116} \ ^{82}$ 41 62 12 20 27 14 10 23 78 112 18 31 ¹⁰⁰ 79 58 37 99 133 39 52 ¹¹³ 92 126 105 84 139 118 97

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What is it? Mathematical Art Math Education?

Outer ring colouring:

For the *n*th node, the colour contains:

red if $n \cong 0 \mod 2$ green if $n \cong 0 \mod 3$ blue if $n \cong 0 \mod 5$



Background colouring:

The shade of grey is based on the "Fibonacci metric", which assigns to n the minimal number of Fibonacci numbers needed to sum to n.



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These patterns continue outwards in interesting ways, here with 15,000 nodes:



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> 3.0 2.5 2.0 1.5 1.0 0.5

> > 0.5

1.0

The pinecone shape

The shape of the pinecone, obtained after lots of tweaking and modifying, is defined as follows:

 $g(u) = 0.21u^{2} + (1 - 0.21\pi)u$ $x(\theta) = 4.5 \sin(g(\theta))$ $y(\theta) = 7.5 \sin(\theta)$

2.0

3.0

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Using that curve we wrap the nodes around to form the pinecone. The shape was tweaked to match a photograph of an (idealised) "real-life" pinecone.

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The scripting language in Second Life is event based, and syntactically similar to Java.



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The final rendering was done by Bathsheba Grossman (www.bathsheba.com) using Rhinoceros 3d, a professional CAD program.



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What is Second Life?

"Second Life is a free online virtual world imagined and created by its Residents."



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What is it? Mathematical Art Math Education?



Total land mass is around 1,800 $\rm km^2$ and approximately 750,000 people log in each month.

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Mathematical Art in Second Life



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"RhombdO" by Bathsheba Grossman.

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Various sculptures by me.



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"Wire Flower" by Suzanne Graves (SL name)

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A projection into 3-space of the Gosset 4_{21} polytope, which is itself a representation of the exceptional Lie group *E*8. By Wizard Gynoid, Desdemona Enfield and Nand Nerd (SL names).

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Wizard was advised by physicist Garrett Lisi (Garrett Netizen in SL).

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The model has since been brought to the real world by Bathsheba Grossman.

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Math Education in Second Life

People also go to lectures in Second Life:



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A lecture by Cleff Karu (SL name) on the history of mathematics.

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Warwick University mathematics department has a presence in Second Life, as do hundreds of universities and colleges worldwide.

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What is it? Mathematical Art Math Education? "Virtual Morocco was a cross-reality service-learning project where Johnson & Wales University students worked with the Ministry of Tourism in Morocco to develop Casablanca island as a tourism promotion tool and a space for cross-cultural collaboration."



Developed by Hilary Mason, Mehdi Moutahir and students.

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What is it? Mathematical Art Math Education? Most uses in the sciences are in museum style exhibits.



Viking Lander model, by Kanker Greenacre (SL Name) at the International Spaceflight Museum.

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A working Turing machine, developed by Kenneth Schweller at Buena Vista University.

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Mathematical exhibits at the New Media Consortium, by me.

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What is it? Mathematical Art Math Education? Przemyslaw Bogacki, a.k.a. Reaso Ning (SL name) has experimented with using Second Life to teach linear algebra at Old Dominion University.



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Pros and Cons to using Second Life in education Pros:

- ► Free to explore and use.
- ► Relatively inexpensive to have a permanent presence.
- Location is irrelevant (good for distance learning etc.).
- Good voice and text communication.
- Very active existing education community.
- 3D virtual classroom interaction works better than other distance learning methods.
- Virtual worlds are *built* on mathematics. Geometric knowledge translates directly into being able to make something.

Cons:

- Technology is still in development: some reliability issues.
- Requires a good graphics card and broadband internet connection.

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No writing on a blackboard!